

Exam - 2020

# Mathematics General

4th semester  $\rightarrow$  MTM 61

Full Marks  $\rightarrow$  45.

Time - 2 Hours.

## Group - A (ALGEBRA - II)

A. Ans Any two

$2 \times 5 = 10$

A.1. a) For three set  $A = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$ ,  $B = \{2, 4, 6, 8, 10\}$

$C = \{1, 3, 5, 7, 9\}$ . Verify that  $A - (B \cup C) = (A - B) \cap (A - C)$

b)  $A = \{p, q, r\}$ ,  $B = \{s, t, u\}$ ,  $C = \{s, u\}$ . Verify that

$$A \times (B - C) = (A \times B) - (A \times C)$$

A.2. a) Let  $(G, \circ)$  be a group. Then prove that

$$(a \circ b)^{-1} = b^{-1} \circ a^{-1} \quad \forall a, b \in G.$$

b) Show that the set of all root of the equation

$x^4 = 1$  form a group under multiplication.

A.3. a) In the real vector space  $\mathbb{R}^3$ ,  $\alpha = (0, 1, 3)$ ,  $\beta = (2, 1, 1)$ ,  $\gamma = (4, 2, 2)$ .

Are they Linearly Independent. Justify.

b) Prove that the set  $S = \{(2, 1, 1), (1, 2, 1), (1, 1, 2)\}$  form

a basis of  $\mathbb{R}^3$ .

## Group - B (Computer)

B. Ans any three :-

$3 \times 6 = 18$

B.1. Write down the full form of the following.

a) CPU

b) ALU

c) MIPER.

d) OMR,

e) OCR.

f) CV.

B.2. Write down the difference between Hardware and software.

B.3. a) Obtain the binary equivalent of the number  $(13.535)_{10}$ .

- b) Find the subtraction  $1101010 - 0101010$ . (2's complement)
- B.4. Write down the flow chart to calculate maximum of three real numbers follows.
- B.5. Write a C program to determine whether a year is a leap year or not.

### Group - C (Probability)

C.

1. Answer any two:-

- 1.a) The probability density function of a continuous distribution is given by  $f(x) = \frac{3}{4}x(2-x)$ ,  $0 < x < 2$ .  
compute the mean and variance.  $6 \times 2 = 12$
- 1.b) The joint probability density function of two random variable X and Y is given by

$$f(x) = 8xy \quad 0 \leq x \leq y, \quad 0 \leq y \leq 1$$

$$= 0, \quad \text{else where.}$$

Determine marginal density function X & Y; check whether X and Y are independent. Also compute  $\text{Var}(X)$  and  $\text{Var}(Y)$ .

- 1.c) Find the Mean and variance of Binomial Distribution.

2. Answer Any one.

$$5 \times 1 = 5$$

- 2.a) State and ~~proved~~ proof the Bayes theorem.
- 2.b) Four dice are thrown. Find the probability that the sum of the number will be 15.